What Do We Learn About Voter Preferences From Conjoint Experiments?

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Forced choice factorial experiments

Randomize features of profiles, ask respondents to choose most preferred

Conjoint experiments have become a standard tool in political science

	Candidate 1	Candidate 2
Number of Children	3	3
Gender	Female	Male
Number of Years in Politics	3 years	8 years
Current Occupation	Mayor	Corporate Lawyer
Age	65	65
Spouse's Occupation	Farmer	Farmer

Based on the limited information above, which of the two candidates would you be more likely to support in the congressional primary?

Candidate 1Candidate 2

Teele, Kalla, and Rosenbluth – APSR (2018)

Forced choice factorial experiments

Randomize features of profiles, ask respondents to choose most preferred The target estimand:

- The Average Marginal Component Effect (AMCE): the effect of varying a feature on the probability a profile is chosen, averaging over all other attributes

Hainmueller, Hopkins, and Yamamoto (2014) - 400+ citations

"respondents prefer candidates who have an Ivy League education and who are not car dealers, Mormon, or fairly old."

Hainmueller, Hopkins, and Yamamoto - PA (2014)

"Americans express a pronounced preference for immigrants who are well educated, are in high-skilled professions, and plan to work upon arrival"

Hainmueller and Hopkins - AJPS (2015)

"In contrast to the observed attributes of actual politicians, voters do not prefer older politicians or celebrities, and are indifferent with regard to dynastic ties and gender."

Horiuchi, Smith, and Yamamoto - PSRM (2018)

"voters and legislators do not seem to hold female candidates in disregard; all else equal, they prefer female to male candidates"

Teele, Kalla, and Rosenbluth - APSR (2018)

Researchers interpret AMCEs in the context of elections



Carnes and Lupu - APSR (2016)



Teele, Kalla, and Rosenbluth - APSR (2018)

Key takeaway

Without additional assumptions on the distribution of preferences, a positive AMCE of X over X' does not imply:

- A majority of respondents prefer X to X^\prime
- A randomly drawn voter prefers X to X', all else equal
- X beats X' in most elections

We describe:

- What the AMCE estimates using a simple example
- AMCE as a preference aggregation rule

We provide:

- Analytic bounds on proportion who prefer X to X^\prime
- Conditions when AMCE corresponds to majority preference

An Example

Preferences over candidate profiles are constructed from:

- Rankings of features (researchers' quantities of interest)
- Weights (e.g., how much an individual cares about party ID relative to gender)

Agnostic about content of preferences

Assume individual rankings over features complete and transitive

Definitions

- Without these assumptions, issues persist

5 voters

2 binary attributes:

- Party ID (Democrat or Republican)
- Gender (Male or Female)

V1	V2	V3	V4	V5
$M \succ F$	$M \succ F$	$M \succ F$	$F \succ M$	$F \succ M$
$R \succ D$	$R \succ D$	$R \succ D$	$D \succ R$	$D \succ R$

V1, V2, and V3 place more weight on candidates' parties

- P >> G

V4 and V5 place more weight on candidates' genders

- G >> P

V1	V2	V3	V4	V5
$M \succ F$	$M \succ F$	$M \succ F$	$\mathbf{F}\succ \mathbf{M}$	$\mathbf{F}\succ \mathbf{M}$
$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$D \succ R$	$D \succ R$

V1	V2	V3	V4	V5
$M \succ F$	$M \succ F$	$M \succ F$	$\mathbf{F}\succ\mathbf{M}$	$\mathbf{F}\succ\mathbf{M}$
$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$D \succ R$	$D \succ R$

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

V1	V2	V3	V4	V5
$M \succ F$	$M \succ F$	$M \succ F$	$\mathbf{F}\succ \mathbf{M}$	$\mathbf{F}\succ\mathbf{M}$
$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$D \succ R$	$D \succ R$

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

V1	V2	V3	V4	V5
$M \succ F$	$M \succ F$	$M \succ F$	$\mathbf{F}\succ \mathbf{M}$	$\mathbf{F}\succ\mathbf{M}$
$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$D \succ R$	$D \succ R$

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

V1	V2	V3	V4	V5
$M \succ F$	$M \succ F$	$M \succ F$	$\mathbf{F}\succ \mathbf{M}$	$\mathbf{F}\succ\mathbf{M}$
$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$D \succ R$	$D \succ R$

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

V1	V2	V3	V4	V5
$M \succ F$	$M \succ F$	$M \succ F$	$\mathbf{F}\succ\mathbf{M}$	$\mathbf{F}\succ\mathbf{M}$
$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$D \succ R$	$D \succ R$

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

V1	V2	V3	V4	V5
$M \succ F$	$M \succ F$	$M \succ F$	$\mathbf{F}\succ\mathbf{M}$	$\mathbf{F}\succ\mathbf{M}$
$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$D \succ R$	$D \succ R$

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

V1	V2	V3	V4	V5
$M \succ F$	$M \succ F$	$M \succ F$	$\mathbf{F}\succ\mathbf{M}$	$\mathbf{F}\succ\mathbf{M}$
$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ \mathbf{D}$	$\mathbf{R}\succ\mathbf{D}$	$D \succ R$	$D \succ R$

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

Tally the number of votes each candidate would receive:

ComparisonV1V2V3V4V5TallyMR, FR

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

ComparisonV1V2V3V4V5TallyMR, FRMR

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

ComparisonV1V2V3V4V5TallyMR, FRMRMRMR

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

ComparisonV1V2V3V4V5TallyMR, FRMRMRMRFR

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

ComparisonV1V2V3V4V5TallyMR, FRMRMRMRFRFR

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

ComparisonV1V2V3V4V5TallyMR, FRMRMRMRFRFR3, 2

Rank	V1	V2	V3	V4	V5
1.	MR	MR	MR	FD	FD
2.	FR	FR	FR	FR	FR
3.	MD	MD	MD	MD	MD
4.	FD	FD	FD	MR	MR

Comparison	V1	V2	V3	V4	V5	Tally
\mathbf{MR}, FR	MR	MR	MR	FR	FR	3, 2
\mathbf{MR}, FD	MR	MR	MR	FD	FD	3, 2
\mathbf{MR}, MD	MR	MR	MR	MD	MD	3, 2
MD, \mathbf{FR}	FR	FR	FR	FR	FR	0,5
\mathbf{MD}, FD	MD	MD	MD	FD	FD	3, 2
\mathbf{FR}, FD	FR	FR	FR	FD	FD	3, 2

$$\underbrace{\bar{Y}(MR, MD)}_{MR' \text{s vote share against } MD} - \underbrace{\bar{Y}(FR, MD)}_{FR' \text{s vote share against } MD} =$$

Comparison	V1	V2	V3	V4	V5	Tally
MR, FR	MR	MR	MR	FR	FR	3, 2
\mathbf{MR}, FD	MR	MR	MR	FD	FD	3, 2
\mathbf{MR}, MD	MR	MR	MR	MD	MD	3, 2
MD, \mathbf{FR}	FR	FR	FR	FR	FR	0, 5
MD, FD	MD	MD	MD	FD	FD	3, 2
\mathbf{FR}, FD	FR	FR	FR	FD	FD	3, 2

 $3/5 \qquad - \bar{Y}(FR, MD) =$

Comparison	V1	V2	V3	V4	V5	Tally
\mathbf{MR}, FR	MR	MR	MR	FR	FR	3, 2
\mathbf{MR}, FD	MR	MR	MR	FD	FD	3, 2
\mathbf{MR}, MD	MR	MR	MR	MD	MD	3, 2
MD, \mathbf{FR}	FR	FR	FR	FR	FR	0, 5
MD, FD	MD	MD	MD	FD	FD	3, 2
\mathbf{FR}, FD	FR	FR	FR	FD	FD	3, 2

$$3/5 - 5/5 = -2/5$$

Comparison	V1	V2	V3	V4	V5	Tally
\mathbf{MR}, FR	MR	MR	MR	FR	FR	3, 2
\mathbf{MR}, FD	MR	MR	MR	FD	FD	3, 2
MR, MD	MR	MR	MR	MD	MD	3, 2
MD, \mathbf{FR}	FR	FR	FR	FR	FR	0, 5
MD, FD	MD	MD	MD	FD	FD	3, 2
\mathbf{FR}, FD	FR	FR	FR	FD	FD	3, 2

$$\bar{Y}(MR, MD) - \bar{Y}(FR, MD) = -2/5$$

$$\bar{Y}(MR, FD) - \bar{Y}(FR, FD) =$$

$$\bar{Y}(MR, MD) - \bar{Y}(FR, MD) = -2/5$$

3/5 - 3/5 = 0

$$\bar{Y}(MR, MD) - \bar{Y}(FR, MD) = -2/5$$

$$\bar{Y}(MR, FD) - \bar{Y}(FR, FD) = 0$$

$$\bar{Y}(MR, MR) - \bar{Y}(FR, MR) = 1/10$$

$$\bar{Y}(MR, FR) - \bar{Y}(FR, FR) = 1/10$$
$\bar{Y}(MR, MD)$	_	$\bar{Y}(FR, MD)$	=	-2/5
$\bar{Y}(MR, FD)$	_	$\bar{Y}(FR,FD)$	=	0
$\bar{Y}(MR, MR)$	_	$\bar{Y}(FR, MR)$	=	1/10
$\bar{Y}(MR, FR)$	_	$\bar{Y}(FR,FR)$	=	1/10
$\bar{Y}(MD, MD)$	_	$\bar{Y}(FD, MD)$	=	1/10
$\bar{Y}(MD,FD)$	—	$\bar{Y}(FD,FD)$	=	1/10
$\bar{Y}(MD, MR)$	—	$\bar{Y}(FD, MR)$	=	0
$\bar{Y}(MD, FR)$	_	$\bar{Y}(FD, FR)$	=	-2/5

$\bar{Y}(MR, MD)$	_	$\bar{Y}(FR, MD)$	=	-2/5
$\bar{Y}(MR, FD)$	_	$\bar{Y}(FR,FD)$	=	0
$\bar{Y}(MR, MR)$	_	$\bar{Y}(FR, MR)$	=	1/10
$\bar{Y}(MR, FR)$	_	$\bar{Y}(FR,FR)$	=	1/10
$\bar{Y}(MD, MD)$	_	$\bar{Y}(FD, MD)$	=	1/10
$\bar{Y}(MD,FD)$	_	$\bar{Y}(FD,FD)$	=	1/10
$\bar{Y}(MD, MR)$	_	$\bar{Y}(FD, MR)$	=	0
$\bar{Y}(MD, FR)$	_	$\bar{Y}(FD,FR)$	=	-2/5
				-2/5

Normalizing this, we get an AMCE of -1/15

We have a negative AMCE of being male Yet we know majority of voters prefer men And we know men win most elections Why?

- AMCE combines direction and strength of preferences
- Correlation between prioritizing gender and a preference for women

Such a correlation structure pervades politics

This is not a sampling issue

ANES

AMCE is a summary statistic that gives us an "average voter" Majorities are decided by median voters, not average Same 5 voters, same preferences as before Include a third feature, $A \in \{O, Y\}$

- Voters 1, 2, and 3 have the weights P >> G >> A
- Voters 4 and 5 have the weights A >> G >> P

No interactions

Produces an AMCE of Male of 1/14

- Opposite sign of AMCE of Male without Age

- 1) May indicate the opposite of majority preference
- 2) Depends on the randomization scheme, even when no interactions

Preference Aggregation

In other words, a preference aggregation rule

- A large literature devoted to study of social choice

AMCE is a preference aggregation rule related to the Borda Count

This connection helps us place bounds on the proportion who prefer a feature

Sketch of Proof

Borda scores of each candidate:

- Borda: Assign last choice a score of zero
- Penultimate choice: score of one
- Top choice: K 1(K := number of profiles)

V1	Borda score
MR	3
FR	2
MD	1
FD	0

Sketch of Proof

Borda scores of each candidate:

- Borda: Assign last choice a score of zero
- Penultimate choice: score of one
- Top choice: K 1(K := number of profiles)

All pairwise comparisons made:

- Last choice never picked when one of the options
- Penultimate choice picked once
- Top choice picked against all others: K 1 times

A candidate's Borda score = # of times that candidate is picked

Borda score of a feature := sum of Borda scores of all profiles with that feature A feature's Borda score = number of times profiles with that feature picked

 \implies Borda score of feature t_1 – Borda score of feature t_0

of times t_1 picked – # of times t_0 picked

$\bar{Y}(MR, MD)$	_	$\bar{Y}(FR, MD)$	=	-2/5
$\bar{Y}(MR, FD)$	_	$\bar{Y}(FR,FD)$	=	0
$\bar{Y}(MR, MR)$	_	$\bar{Y}(FR, MR)$	=	1/10
$\bar{Y}(MR,FR)$	_	$\bar{Y}(FR,FR)$	=	1/10
$\bar{Y}(MD, MD)$	_	$\bar{Y}(FD, MD)$	=	1/10
$\bar{Y}(MD,FD)$	_	$\bar{Y}(FD,FD)$	=	1/10
$\bar{Y}(MD, MR)$	_	$\bar{Y}(FD, MR)$	=	0
$\bar{Y}(MD, FR)$	—	$\bar{Y}(FD, FR)$	=	-2/5
19/5	_	21/5	=	-2/5

Borda score of a feature := sum of Borda scores of all profiles with that feature A feature's Borda score = number of times profiles with that feature picked

 \implies Borda score of feature t_1 – Borda score of feature t_0

of times t_1 picked – # of times t_0 picked

Proposition 1: Borda scores are proportional to AMCE.

Borda score of a feature := sum of Borda scores of all profiles with that feature A feature's Borda score = number of times profiles with that feature picked

 \implies Borda score of feature t_1 – Borda score of feature t_0

= # of times t_1 picked – # of times t_0 picked

AMCE \times some constant

- 1) Borda fails to indicate the majority preference
- 2) Borda fails the independence of irrelevant alternatives

Analytical Bounds

Bounds on fractions of people who prefer a feature as a function of:

- The AMCE estimate
- Number of possible profiles

Proposition 2: Bounds on the fraction who prefer t_1 to t_0 .

Given AMCE of $\pi(t_1, t_0)$, fraction who prefer t_1 to t_0 lies in interval

$$\left[\max\left\{0, \frac{\pi(t_1, t_0)2(K-1) + 2}{K+2}\right\}, \min\left\{1, \frac{\pi(t_1, t_0)2(K-1) + K}{K+2}\right\}\right]$$

Sketch of proof for lower bound: (symmetric for upper bound)

- Suppose respondents who prefer t_1 give highest weight and those who prefer t_0 give lowest weight
- Leads to maximum possible Borda score for t_1 and minimum possible Borda score for t_0

Those who prefer t_1 maximally give $\left(\frac{K}{2}\right)^2$ more points to t_1 than t_0 Those who prefer t_0 minimally give $\frac{K}{2}$ more points to t_0 than t_1

AMCE
$$\propto$$
 (fraction who prefers t_1) $\left(\frac{K}{2}\right)^2$ + (fraction who prefers t_0) $\left(-\frac{K}{2}\right)$

Inverting this yields the lower bound.

General bounds























Analytical Bounds APSR/AJPS/JOP

Paper	AMCE (π)	K	au	Bounds
APSR				
Ward (2019)	-0.18	6,840	5	[0, 0.77]
Auerbach and Thachil (2018)	0.13	1,296	3	[0.20, 1]
Hankinson (2018)	-0.09	6,144	4	[0, 0.88]
Teele, Kalla, and Rosenbluth (2018)	0.15	864	4	[0.20, 1]
Carnes and Lupu (2016)	0.09	32	2	[0.22, 1]
JOP				
Newman and Malhotra (2018)	0.35	120,960	9	[0.39, 1]
Ballard-Rosa, Martin, and Scheve (2016)	-0.24	38,400	4	[0, 0.68]
Mummolo and Nall (2016)	0.11	3,456	4	[0.15, 1]
Mummolo (2016)	0.30	6	2	[0.63, 1]
AJPS				
Hemker and Rink (2017)	0.33	155	2	[0.66, 1]
Huff and Kertzer (2017)	0.19	108,000	6	[0.23, 1]

Analytical Bounds APSR/AJPS/JOP

Paper	AMCE (π)	K	τ	Bounds
APSR				
Ward (2019)	-0.18	6,840	5	[0, 0.77]
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AJPS				
Hemker and Rink (2017)	0.33	155	2	[0.66, 1]
Huff and Kertzer (2017)	0.19	108,000	6	[0.23, 1]

When can the AMCE capture majority preference?

Sketch of Proof

Suppose weights are distributed identically across supporters and opponents In expectation, each t_1 supporter gives as many more points to t_1 than t_0 as an opponent takes away from it

Thus, we can write

AMCE \propto fraction who prefers t_1 – fraction who prefers t_0

AMCE combines intensity and direction of preferences to give an "average voter" In many applications, we want to discern the two

To capture electoral majorities:

- Attributes binary
- Total number of profiles low
- But note that small effect sizes still won't detect majorities

External validity requires inclusion of all relevant attributes

Recover weights assigned to attributes

- Evaluate homogeneous weights assumption

Develop approaches that decouple direction from intensity

- Estimate a model of voting
- Uncover marginal willingness to pay

Use social choice theory to inform our understanding of empirical estimands
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Maximal points to t_1



Minimal points to t_0

$$\underbrace{\underbrace{t_0\alpha\beta\gamma}_{K-1} \succ \underbrace{t_1\alpha\beta\gamma}_{K-2}}_{1} \succ \underbrace{\underbrace{t_0\alpha'\beta\gamma}_{K-3} \succ \underbrace{t_1\alpha'\beta\gamma}_{K-4} \succ \ldots \succ \underbrace{t_0\alpha'\beta'\gamma'}_{1} \succ \underbrace{t_1\alpha'\beta'\gamma'}_{0}}_{1}$$

$$\underbrace{\underbrace{t_0\alpha\beta\gamma}_{K-1} \succ \underbrace{t_1\alpha\beta\gamma}_{K-2} \succ \underbrace{t_0\alpha'\beta\gamma}_{K-3} \succ \underbrace{t_1\alpha'\beta\gamma}_{K-4} \succ \ldots \succ \underbrace{t_0\alpha'\beta'\gamma'}_{1} \succ \underbrace{t_1\alpha'\beta'\gamma'}_{0}$$

$$\underbrace{\underbrace{t_0\alpha\beta\gamma}_{K-2} \succ \underbrace{t_1\alpha\beta\gamma}_{K-2} \succ \underbrace{t_1\alpha'\beta\gamma}_{K-4} \succ \ldots \succ \underbrace{t_0\alpha'\beta'\gamma'}_{1} \succ \underbrace{t_1\alpha'\beta'\gamma'}_{0}$$

$$\underbrace{\underbrace{t_0\alpha\beta\gamma}_{K-2} \vdash \underbrace{t_1\alpha\beta\gamma}_{K-2} \succ \underbrace{t_1\alpha'\beta\gamma}_{K-4} \succ \ldots \succ \underbrace{t_0\alpha'\beta'\gamma'}_{1} \succ \underbrace{t_1\alpha'\beta'\gamma'}_{0}$$

Fraction of respondents who prefer t_1 over t_0 , given an AMCE estimate of $\pi(t_1, t_0)$, must be in the interval

$$y \in \left[\max\left\{ \frac{\pi(t_1, t_0)\tau(K-1) + \tau}{K(\tau - 1) + \tau}, 0 \right\}, \\ \min\left\{ \frac{\pi(t_1, t_0)\tau(K-1) + K(\tau - 1)}{K(\tau - 1) + \tau}, 1 \right\} \right]$$

where au is the number of distinct values the attribute of interest can take.

AMCE of Male 1,000 Samples of 3 Questions Per Voter



- Complete ($x \succeq y$, $y \succeq x$ or both)
- Transitive (if $x \succeq y \& y \succeq z$, then $x \succeq z$)

Lemma 2: With no interactions and binary attributes, a profile has the highest Borda score if and only if all its features have the highest Borda scores for their respective attributes.

Sketch of proof

Definition: (No interactions) Voter *i*'s preferences have no interactions when for all $t_1, t_0, \alpha, \beta, \alpha'$, and β' , we have

$$t_1 \alpha \beta \succ t_0 \alpha \beta \iff t_1 \alpha' \beta' \succ t_0 \alpha' \beta'.$$

No interactions
$$\implies b_i(t_1\alpha\beta) - b_i(t_1\alpha'\beta') = b_i(t_0\alpha\beta) - b_i(t_0\alpha'\beta')$$

$$\iff \sum_{i \in N} b_i(t_1 \alpha \beta) - \sum_{i \in N} b_i(t_0 \alpha \beta) = \sum_{i \in N} b_i(t_1 \alpha' \beta') - \sum_{i \in N} b_i(t_0 \alpha' \beta')$$

Suppose $t_1 lpha eta$ is the profile with the highest Borda score

$$\iff \sum_{i \in N} b_i(t_1 \alpha \beta) - \sum_{i \in N} b_i(t_0 \alpha \beta) \ge 0$$

$$\iff \sum_{i \in N} b_i(t_1 \alpha' \beta') - \sum_{i \in N} b_i(t_0 \alpha' \beta') \ge 0 \text{ for all } \alpha', \beta'$$

Recall $B_i(t_1) = \sum_{\alpha, \beta} \sum_{i \in N} b_i(t_1 \alpha \beta)$
$$\iff B_i(t_1) \ge B_i(t_0)$$

Journalists also interpret conjoints in the context of elections



Direction and intensity: Feminism



Question	Correlation	χ^2	# of categories
Favor allowing use of bathrooms of identified gender	-0.258 (0.000)	309.2 (0.000)	3
Favor torture for suspected terrorists	-0.246 (0.000)	147.8 (0.000)	3
Favor allowing Syrian refugees into US	-0.246 (0.000)	203.6 (0.000)	3
Favor 2010 health care law	-0.182 (0.000)	125.4 (0.000)	3
Support preferential hiring/promotion of blacks	-0.173 (0.000)	104.9 (0.000)	2
Favor building a wall with Mexico	-0.129 (0.000)	73.6 (0.000)	3
Favor affirmative action in universities	-0.098 (0.000)	15.7 (0.000)	2
Favor sending troops to fight ISIS	-0.080 (0.000)	21.7 (0.000)	3
Think economy has gotten better since 2008	-0.065 (0.000)	13.1 (0.000)	2
Agree that children brought illegally should be sent back	-0.025 (0.103)	2.7 (0.260)	3
Think government should make it harder to own a gun	-0.024 (0.289)	7.1 (0.069)	4
Approve of House incumbent	-0.013 (0.472)	0.5 (0.497)	2
Favor ending birthright citizenship	-0.011 (0.550)	1.6 (0.459)	3
Favor requiring provision of services to same-sex couples	0.020 (0.199)	8.8 (0.012)	3
Favor laws protecting gays against job discrimination	0.110 (0.000)	49.9 (0.000)	2
Think government should take more action on climate change	0.132 (0.000)	66.2 (0.000)	3
Favor requiring employers to give paid leave to new parents	0.149 (0.000)	29.1 (0.000)	2
Favor vaccines in schools	0.174 (0.000)	97.7 (0.000)	3
Support requiring equal pay for men and women	0.201 (0.000)	145.2 (0.000)	3
Favor the death penalty	0.211 (0.000)	184.2 (0.000)	2
Believe benefits of vaccination outweigh risks	0.275 (0.000)	251.4 (0.000)	3
The term 'feminist' describes you extremely/very well	0.328 (0.000)	115.3 (0.000)	5

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